

## DAMPING FUNCTION OF BACK TO BACK HVDC BASED VOLTAGE SOURCE CONVERTER

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**Abstract-** This paper presents the establishment of linearised Phillips-Heffron model of a power system installed HVAC parallel-connected with a Back To Back High Voltage Direct Current based voltage source converter (BtB VSC HVDC). The use of the supplementary controllers of a BtB VSC HVDC to damp low frequency oscillations in a weakly connected system is considered. The potential of the BtB VSC HVDC supplementary controllers to enhance the dynamic stability is evaluated using damping function.

**Keywords:** Phillips-Heffron Model, Back To Back, HVAC, BtB VSC HVDC.

### I. INTRODUCTION

As power demand grows rapidly and expansion in transmission and generation is restricted with the limited availability of resources and the strict environmental constraints, power systems are today much more loaded than before. This causes the power systems to be operated near their stability limits [1]. Power system stabilizers (PSSs) aid in maintaining power system stability and improving dynamic performance by providing a supplementary signal to the excitation system [2].

However, PSSs may adversely affect voltage profile, may result in leading power factor, and may not be able to suppress oscillations resulting from severe disturbances, especially those three-phase faults which may occur at the generator terminals [1].

The availability of Flexible AC Transmission System (FACTS) controllers, such as Static VAR Compensators (SVC), Thyristor Control Series Compensators (TCSC), Static Synchronous Compensators (STATCOM), and Unified Power Flow Controller (UPFC), have led their use to damping oscillations [3-5].

Extremely fast control action associated with FACTS-device operations, they have been very promising candidates for utilization in power system damping enhancement. It has been observed that utilizing a feedback supplementary control, in addition to the FACTS-device primary control, can considerably improve system damping and can also improve system voltage profile, which is advantageous over PSSs [1].

Recently HVDC systems have greatly increased. They interconnect large power systems offering numerous technical and economic benefits. This interest results from functional characteristics and performance that include for example nonsynchronous interconnection, control of power flow and modulation to increase stability limits [6]. It is well known that the transient stability of the AC systems in a composite AC-DC system can be improved by taking advantage of the fast controllability of HVDC converters [7-12]. There are, therefore, good reasons for constructing HVDC links in close proximity to HVAC lines.

In this paper a novel approach is presented to model parallel-connected HVAC and BtB VSC HVDC systems. In addition to the state-space representation, a block diagram representation is formed to analyze the system stability characteristics. By this modeling approach, it is possible to analyze the small-signal stability of the system and low-frequency oscillation phenomena with the synchronous machine.

### II. CONFIGURATION OF POWER SYSTEM

Figure 1 shows a SMIB system equipped with a HVDC. The four input control signals to the HVDC are  $M_r, PH_r, M_i, PH_i$  where  $M_r, M_i$  are the amplitude modulation ratio and  $PH_r, PH_i$  are phase angle of the control signals of each VSC respectively.

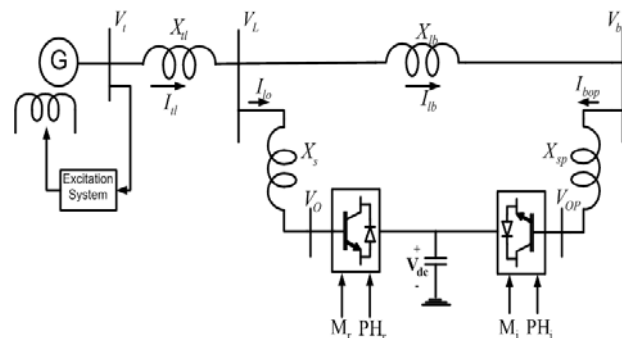


Figure 1. Configuration of case study

By applying Park's transformation and neglecting the resistance and transients of the coupling transformers, the HVDC can be modeled:

$$\begin{bmatrix} V_{Ld} \\ V_{Lq} \end{bmatrix} = \begin{bmatrix} 0 & -X_s \\ X_s & 0 \end{bmatrix} \begin{bmatrix} I_{lod} \\ I_{loq} \end{bmatrix} + \begin{bmatrix} \frac{M_r V_{dc} \cos(PH_r)}{2} \\ \frac{M_r V_{dc} \sin(PH_r)}{2} \end{bmatrix} \quad (1)$$

$$\begin{bmatrix} V_{bd} \\ V_{bq} \end{bmatrix} = \begin{bmatrix} 0 & -X_{sp} \\ X_{sp} & 0 \end{bmatrix} \begin{bmatrix} I_{bopd} \\ I_{bopq} \end{bmatrix} + \begin{bmatrix} \frac{M_i V_{dc} \cos(PH_i)}{2} \\ \frac{M_i V_{dc} \sin(PH_i)}{2} \end{bmatrix} \quad (2)$$

$$C_{dc} \dot{V}_{dc} = \left[ \frac{M_r}{2} (I_{lod} \cos(PH_r) + I_{loq} \sin(PH_r)) + \frac{M_i}{2} (I_{bopd} \cos(PH_i) + I_{bopq} \sin(PH_i)) \right] \quad (3)$$

where  $V_L, V_b, I_{lo}$  and  $I_{bo}$  are the middle bus voltage, infinite bus voltage, flowed current to rectifier and inverter respectively.  $C_{dc}$  And  $V_{dc}$  are the DC link capacitance and voltage, respectively.

The non-linear model of the SMIB system of Figure1 is:

$$\dot{\delta} = \omega_b \omega \quad (4)$$

$$\dot{\omega} = \frac{(P_m - P_e - D\omega)}{M} \quad (5)$$

$$\dot{E}'_q = \frac{(E_{fd} - (x_d - x'_d)I_{td} - E'_q)}{T'_{do}} \quad (6)$$

$$\dot{E}_{fd} = \frac{(K_A(V_{ref} - V_t) - E_{fd})}{T_A} \quad (7)$$

where  $P_e = V_{td} I_{td} + V_{tq} I_{tq}$ ,  $V_t = \sqrt{V_{td}^2 + V_{tq}^2}$ ,  $V_{td} = x_q I_{tq}$ ,  $V_{tq} = E'_q - x'_d I_{td}$ ,  $I_{td} = I_{lod} + I_{bd}$ ,  $I_{tq} = I_{loq} + I_{bq}$  and  $P_m$  and  $P_e$  are the input and output power, respectively;  $M$  and  $D$  the inertia constant and damping coefficient, respectively;  $\omega_b$  the synchronous speed;  $\delta$  and  $\omega$  the rotor angle and speed, respectively;  $E'_q, E_{fd}$  and  $V_t$  the generator internal, field and terminal voltages, respectively;  $T'_{do}$  the open circuit field time constant;  $X_d, X'_d$  and  $X_q$  the d-axis, d-axis transient reactance, and q-axis reactance, respectively;  $K_A$  and  $T_A$  the exciter gain and time constant, respectively;  $V_{ref}$  the reference voltage. Also, from Figure1 we have:

$$\bar{V}_t = jX_{tl} \bar{I}_{tl} + \bar{V}_l \quad (8)$$

$$\bar{V}_t = jX_{tl} \bar{I}_{tl} + jX_{lb} \bar{I}_{lb} + \bar{V}_b \quad (9)$$

$$\bar{I}_{lb} = \bar{I}_{tl} - \frac{\bar{V}_t - jX_{tl} \bar{I}_{tl} - \bar{V}_o}{jX_s} \quad (10)$$

Where  $\bar{I}_{tl}$ ,  $\bar{V}_o$ ,  $\bar{I}_{lb}$  and  $\bar{V}_b$  are the armature current, rectifier voltage, infinite bus current and voltage respectively. From (8)-(10) we can have:

$$\bar{I}_{tlq} = \frac{\frac{X_{lb} M_r}{X_s} V_{dc} \cos(PH_r) + V_b \sin(\delta)}{ZX_q + A} \quad (11)$$

$$\bar{I}_{tld} = \frac{ZE'_q - \frac{X_{lb} M_r}{X_s} V_{dc} \sin(PH_r)}{ZX'_d + A} - \frac{-V_b \cos(\delta)}{ZX'_d + A} \quad (12)$$

And for inverter side:

$$\bar{I}_{bopd} = \frac{V_b \cos(\delta) - \frac{M_i}{2} V_{dc} \sin(PH_i)}{X_{sp}} \quad (13)$$

$$\bar{I}_{bopq} = -\frac{V_b \sin(\delta) - \frac{M_i}{2} V_{dc} \cos(PH_i)}{X_{sp}} \quad (14)$$

By linearising (1)-(7), (11)-(14):

$$\dot{\Delta\delta} = \omega_b \Delta\omega \quad (15)$$

$$\dot{\Delta\omega} = \frac{(\Delta P_m - \Delta P_e - D\Delta\omega)}{M} \quad (16)$$

$$\dot{\Delta E}'_q = \frac{(\Delta E_{fd} - (x_d - x'_d)\Delta I_{td} - \Delta E'_q)}{T'_{do}} \quad (17)$$

$$\dot{\Delta E}_{fd} = \frac{(K_A \Delta V_t - \Delta E_{fd})}{T_A} \quad (18)$$

where

$$\dot{\Delta V}_t = K_5 \Delta\delta + K_6 \Delta E'_q + K_{Vdc} \Delta V_{dc} + K_{VM_r} \Delta M_r + K_{VPH_r} \Delta PH_r \quad (19)$$

$$\Delta P_e = K_1 \Delta\delta + K_2 \Delta E'_q + K_{pdc} \Delta V_{dc} + K_{pMr} \Delta M_r + K_{pPH_r} \Delta PH_r \quad (20)$$

$$\Delta E'_q = K_3 \Delta E'_q + K_4 \Delta\delta + K_{qPH_r} \Delta PH_r + K_{qMr} \Delta M_r + K_{qdc} \Delta V_{dc} \quad (21)$$

$$\dot{\Delta V}_{dc} = q_1 \Delta\delta + q_2 \Delta E'_q + q_3 \Delta V_{dc} + q_4 \Delta M_r + q_5 \Delta PH_r + q_6 \Delta M_i + q_7 \Delta PH_i \quad (22)$$

Substitute (19)-(22) in (15)-(18) we can obtain the state variable of the power system installed with the BtB VSC HVDC to be in Equation (23) where  $\Delta M_i, \Delta M_r, \Delta PH_i$  and  $\Delta PH_r$  are the linearization of the input control signals of the BtB VSC HVDC. The linearised dynamic model of (23) can be shown by Figure 2.

$$\begin{bmatrix} \dot{\Delta\delta} \\ \dot{\Delta\omega} \\ \dot{\Delta E'_q} \\ \dot{\Delta E'_{fd}} \\ \dot{\Delta V_{dc}} \end{bmatrix} = \begin{bmatrix} 0 & \omega_b & 0 & 0 & 0 \\ -\frac{K_1}{M} & -\frac{D}{M} & -\frac{K_2}{M} & 0 & -\frac{K_{pdc}}{M} \\ \frac{K_4}{T'_{do}} & 0 & -\frac{K_3}{T'_{do}} & \frac{1}{T'_{do}} & -\frac{K_{qdc}}{M} \\ -\frac{K_A K_A}{T_A} & 0 & -\frac{K_A K_6}{T_A} & -\frac{1}{T_A} & -\frac{K_A K_{Vdc}}{T_A} \\ q_1 & 0 & q_2 & 0 & q_3 \end{bmatrix} \begin{bmatrix} \Delta\delta \\ \Delta\omega \\ \Delta E'_q \\ \Delta E'_{fd} \\ \Delta V_{dc} \end{bmatrix} \quad (23)$$

$$+ \begin{bmatrix} 0 & 0 & 0 & 0 \\ -\frac{K_{pMr}}{M} & -\frac{K_{pPHr}}{M} & 0 & 0 \\ -\frac{K_{qMr}}{T'_{do}} & -\frac{K_{qPHr}}{T'_{do}} & 0 & 0 \\ -\frac{K_A K_{VMr}}{T_A} & -\frac{K_A K_{VPHr}}{T_A} & 0 & 0 \\ q_4 & q_5 & q_6 & q_7 \end{bmatrix} \begin{bmatrix} \Delta M_r \\ \Delta PH_r \\ \Delta M_i \\ \Delta PH_i \end{bmatrix}$$

In this figure  $K_{pu}, K_{qu}, K_{vu}, K_q$  and  $\Delta U$  are defined below:

$$K_{pu} = [K_{pMr}, K_{pPHr}, 0, 0]$$

$$K_{qu} = [K_{qMr}, K_{qPHr}, 0, 0]$$

$$K_{vu} = [K_{VMr}, K_{VPHr}, 0, 0]$$

$$K_q = [q_4, q_5, q_6, q_7]$$

$$\Delta U = [\Delta M_r, \Delta PH_r, \Delta M_i, \Delta PH_i]$$

It can be seen that the configuration of the Phillips-Heffron model is exactly the same as that installed with SVC, TCSC, TCPS, UPFC and STATCOM.

Also from (23) it can be seen that there are four choice of input control signals of the BtB VSC HVDC to superimpose on the damping function of the BtB VSC HVDC  $\Delta M_i, \Delta M_r, \Delta PH_i$  and  $\Delta PH_r$ . Therefore, in designing the damping controller of the BtB VSC HVDC, besides setting its parameters, the selection of the input control signal of the BtB VSC HVDC to superimpose on the damping function of the BtB VSC HVDC is also important.

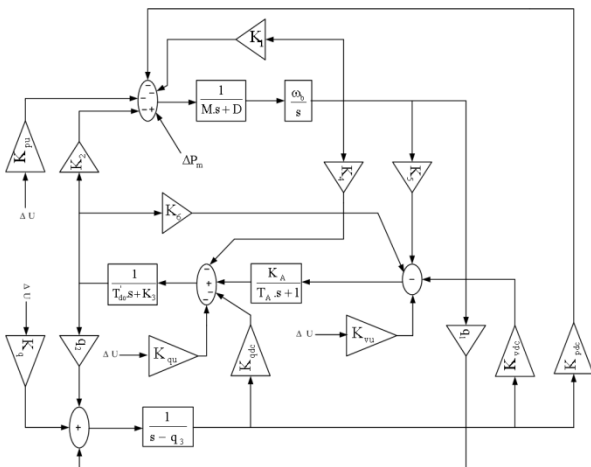


Figure 2. Phillips-Heffron model of power system installed with HVDC

### III. BTB VSC HVDC DAMPING FUNCTION

The linearised model of the power system installed with the BtB VDC HVDC can be expressed by Figure 3 [13], where  $H(s)$  is the transfer function of the HVDC damping controller. From Figure 3 we can obtain the electric torque provided by the HVDC damping controller to the electromechanical oscillation loop of the generator to be:

$$\Delta T_{HVDC} = \frac{K_c(\lambda_0)K_0(\lambda_0)H(\lambda_0)}{1 - K_{IL}(\lambda_0)H(\lambda_0)} \Delta\omega \quad (24)$$

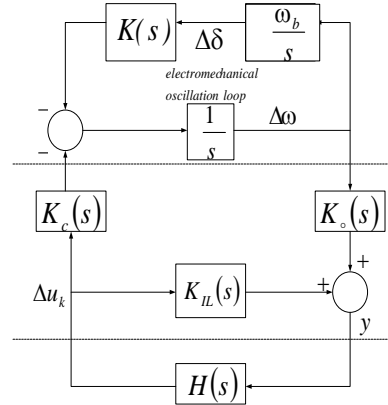


Figure 3. Closed-loop system installed with UPFC damping controller

An ideal UPFC damping controller should contribute a pure positive damping torque to the electromechanical oscillation loop with  $\Delta T_{HVDC} = D_{HVDC} \Delta\omega$  that is:

$$D_{HVDC} = \frac{K_c(\lambda_0)K_0(\lambda_0)H(\lambda_0)}{1 - K_{IL}(\lambda_0)H(\lambda_0)} \quad (25)$$

which results in:

$$D_{HVDC} = [K_c(\lambda_0)K_0(\lambda_0) + D_{IPFC}K_{IL}(\lambda_0)]H(\lambda_0) = F(\lambda_0)H(\lambda_0) \quad (26)$$

$F(\lambda_0)$  which is named as the forward path of the BtB VSC HVDC damping controller, has a decisive influence on the effectiveness of the HVDC damping controller.

If we assume the set of the operating conditions of the power system is  $\Omega(\mu)$ ,  $F(\lambda_0)$  can be denoted as the function of system operating condition  $\mu$  and input control signal of the HVDC  $u_k$ . The criterion of the selection can be [14]:

$$\mu_{selected} = \min_{\mu} F(\lambda_0, \mu, u_k), \mu \in \Omega(\mu) \quad (27)$$

$$u_{selected} = \max_{u_k} F(\lambda_0, \mu_{selected}, u_k) \quad (28)$$

$$u_k \in \{M_r, M_i, PH_r, PH_i\}$$

$$u_{selected} = \min_{u_k} \{ \max_{\mu} F(\lambda_0, \mu, u_k) - \min_{\mu} F(\lambda_0, \mu, u_k) \}$$

$$u_k \in \{M_r, M_i, PH_r, PH_i\}, \mu \in \Omega(\mu) \quad (29)$$

Equation (27) requires that the operating condition, where the HVDC damping control is least effective, is selected for the design of the controller.

- For the efficient operation of the HVDC damping function. The required damping should be provided at minimum control cost.

- A good design of damping controller requires that it provides a steady damping over all the range of power system operating conditions.

Furthermore, from Equation 26 we can see that the phase compensation method can be used to set the parameters of the HVDC damping controller.

**IV. SIMULATION RESULTS**

Power system information is given in appendix A. constant coefficients in (23) are calculated according information's who given in appendix B. For given information, characteristic equation is:

$$\Delta(s) = s^5 + 67.13s^4 + 684.7s^3 + 799.9s^2 + 9089s + 28180$$

with poles:

$$-54.8593, 1.2442 \pm 3.8027j, -2.6505, -12.1114$$

According above, there are two poles with positive real part and power system is unstable (for  $\Delta P_e = 0.05$ )

Figure 4 shows the damping of the oscillation mode over the  $\Omega(\mu)$ . It can be seen that, at the heavy load operating condition, the oscillation mode is of poorest damping. Therefore this operating condition is selected to design the damping controller.

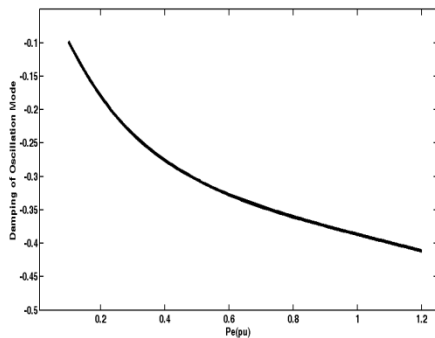


Figure 4. Damping of oscillation mode over the operating condition

The results of calculation of the forward path  $F(\lambda)$  over  $\Omega(\mu)$  as shown by Figure 5.

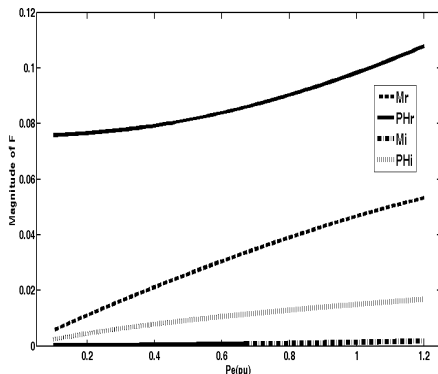


Figure 5. Magnitude of  $F(\lambda)$  over  $\Omega(\mu)$

➤ With  $u_k = M_i$  we have  $F(\lambda) \approx 0$  over  $\Omega(\lambda)$ . Therefore, the oscillation mode controllability is not controllable if the input control signal is chosen to be  $M_i$ . In the following  $M_i$  will not be included in the discussion.

➤ According to the criteria of Equation (26), it can be seen that the operating condition to be selected for the design of the HVDC damping controller is  $P_e = 0.1pu$ .

➤ Figure 5, indicate  $u_k = PH_r$  is most effective input control signal. So the criteria of Equation 28 lead to the selection of the input control signal for the UPFC damping controller as  $u_k = PH_r$ .

The results of applying the criteria of Equation 29 are: with  $u_k = PH_r$ :

$$\frac{\max_{\mu} F(\lambda_0, \mu, u_k) - \min_{\mu} F(\lambda_0, \mu, u_k)}{\min_{\mu} F(\lambda_0, \mu, u_k)} = 0.44$$

with  $u_k = M_r$ :

$$\frac{\max_{\mu} F(\lambda_0, \mu, u_k) - \min_{\mu} F(\lambda_0, \mu, u_k)}{\min_{\mu} F(\lambda_0, \mu, u_k)} = 7.66$$

with  $u_k = PH_i$ :

$$\frac{\max_{\mu} F(\lambda_0, \mu, u_k) - \min_{\mu} F(\lambda_0, \mu, u_k)}{\min_{\mu} F(\lambda_0, \mu, u_k)} = 5.8$$

Therefore, with  $u_k = PH_r$ , the HVDC damping controller provides the smoothest damping to the oscillation mode. The final result of selection is:

$$\mu_{selected} : P_e = 0.1$$

$$u_k = PH_r$$

According to Figure 5 in  $\mu_{selected}$ , magnitude of  $F$  is very low. With attention to Equation 26, this reason decrease  $D_{HVDC}$ . So we select  $\mu : P_e = 0.9pu$  for damping controller designing. Using phase compensation method for damping controller results:

Table 1. Parameters of designed controllers

	$M_r$	$PH_r$	$PH_i$
$T_1$	0.31	0.19	6.2
$T_2$	0.36	0.59	0.018
$K_{dc}$	-60.91	-72.679	9.542

To assess the effectiveness of the damping controller two different conditions are considered according Table 2. Rotor speed deviation and electrical power for suddenly change in mechanical power ( $\Delta P_m = 0.05$ ) is shown in Figure 6.

Table 2. Load condition

Load condition	$P_e(pu)$	$Q_e(pu)$
$\mu_1$	0.9	0.015
$\mu_2$	1.1	0.3

Designed controllers are applied to every input in Figure 2 individually. It is observed that if controller is applied to  $\Delta PH_r$ , rotor speed oscillation is damped better than others input. This supplementary controller is caused the system stability and damping oscillations.

## V. CONCLUSIONS

In this paper, a dynamic model for a AC-DC power system is considered and damping controller is designed for improve power system stability and oscillation damping. Damping function is defined and has been employed to evaluate the oscillation mode controllability to the four BtB VSC HVDC input. Results illustrated that the oscillation mode has best controllability via the fire angle of rectifier.

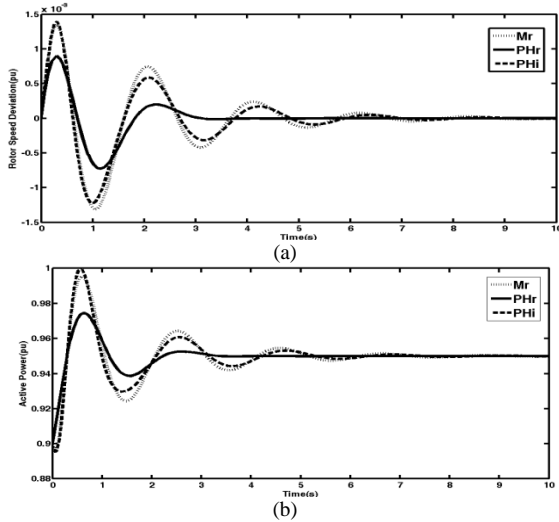


Figure 6.  $\mu_1$  condition (a) Rotor speed deviation (b) Active power

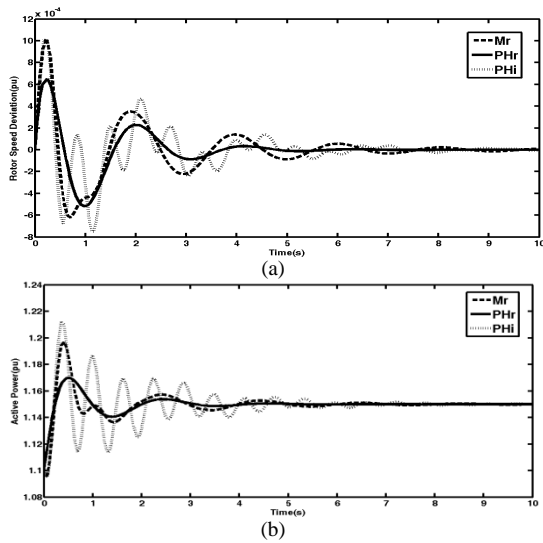


Figure 7.  $\mu_2$  condition (a) Rotor speed deviation (b) Active power

## APPENDICES

### Appendix 1

The test system parameters are:

Machine  $X_d = 1, X_q = 0.6, X'_d = 0.3, D = 0, M = 8,$   
 and  
 exciter:  $T'_{do} = 5.044, freq = 60, v_{ref} = 1, K_A = 120,$   
 $T_A = 0.015$

Transmission line and transformer reactance:  $X_{tl} = 0.15, X_{lb} = 0.6,$   
 $X_{sp} = X_s = 0.15$

BtB VSC HVDC:  $V_{dc} = 3, C_{dc} = 1$

### Appendix 2

Coefficients are:

$$Z = 1 + \frac{X_{lb}}{X_s}, A = X_{tl} + X_{lb} + \frac{X_{tl}}{X_s},$$

$$[A] = A + ZX'_d, [B] = A + ZX_q$$

$$C_1 = \frac{V_b \cos(\delta)}{[B]}, C_2 = -\frac{X_{lb} M_r V_{dc} \sin(PHr)}{2X_s [B]}$$

$$C_3 = \frac{X_{lb} V_{dc} \cos(PHr)}{2X_s [B]}, C_4 = \frac{X_{lb} M_r \cos(PHr)}{2X_s [B]}$$

$$C_5 = \frac{Z}{A}, C_6 = \frac{V_b \sin(\delta)}{[A]}$$

$$C_7 = -\frac{X_{lb} M_r V_{dc} \cos(PHr)}{2X_s [A]}, C_8 = -\frac{X_{lb} V_{dc} \sin(PHr)}{2X_s [A]}$$

$$C_9 = -\frac{X_{lb} M_r V_{dc} \cos(PHr)}{2X_s [A]}, C_b = E'_q + (X_q - X'_d)$$

$$C_a = (X_q - X'_d) I_{tlq}, K_1 = C_b C_1 + C_a C_6$$

$$K_2 = I_{tlq} (1 + (X_q - X'_d) C_5), K_{pdc} = C_b C_4 + C_a C_9$$

$$K_{pMr} = C_b C_3 + C_a C_8, K_{pPHr} = C_b C_2 + C_a C_7$$

$$X_d - X'_d = J, K_3 = 1 + J C_5, K_4 = J C_6, K_{qPHr} = J C_7$$

$$K_{qMr} = J C_8, K_{qdc} = J C_9, L = \frac{1}{V_t}$$

$$K_5 = L(V_{td} X_q C_1 - V_{tq} X'_d C_6)$$

$$K_6 = L V_{tq} (1 - X'_d C_5), K_{Vdc} = L(V_{td} X_q C_4 - V_{tq} X'_d C_9)$$

$$K_{VMr} = L(V_{td} X_q C_3 - V_{tq} X'_d C_8)$$

$$K_{VPHr} = L(V_{td} X_q C_2 - V_{tq} X'_d C_7), E = \frac{X'_d + X_{tl}}{X_s}$$

$$G = \frac{\sin(PHr)}{X_s}, C_{10} = \frac{1}{X_s} (-(X'_d + X_{tl}) C_5 + 1)$$

$$C_{11} = -E C_6, C_{12} = -(E C_7 + \frac{M_r V_{dc} \cos(PHr)}{2X_s})$$

$$C_{13} = -(E C_8 + \frac{G V_{dc}}{2}), C_{14} = -(G \frac{M_r}{2} + E C_9)$$

$$W = \frac{X_q + X_{tl}}{X_s}, C_{15} = -W C_1$$

$$C_{16} = -(W C_2 + \frac{M_r V_{dc} \sin(PHr)}{2X_s}),$$

$$C_{17} = -(W C_4 - \frac{M_r \cos(PHr)}{2X_s}), P_1 = -\frac{V_b \sin(\delta)}{X_{sp}}$$

$$C_{18} = -(W C_3 - \frac{V_{dc} \cos(PHr)}{2X_s}), P_2 = -\frac{M_i V_{dc} \cos(PHi)}{2X_{sp}}$$

$$P_3 = -\frac{M_i \sin(PHi)}{2X_{sp}}, P_4 = -\frac{V_{dc} \sin(PHi)}{2X_{sp}}$$

$$P_5 = -\frac{V_b \cos(\delta)}{X_{sp}}, P_6 = -\frac{M_i V_{dc} \sin(PHi)}{2X_{sp}}$$

$$P_7 = \frac{M_i \cos(PHi)}{2X_{sp}}, P_8 = \frac{V_{dc} \cos(PHi)}{2X_{sp}}$$

$$P_9 = \frac{I_{lod} \cos(PHr) + I_{loq} \sin(PHr)}{2C_{dc}}$$

$$P_{10} = \frac{I_{bopd} \cos(PHi) + I_{lopq} \sin(PHi)}{2C_{dc}}$$

$$P_{11} = \frac{M_r \cos(PHr)}{2C_{dc}}, P_{12} = -\frac{M_r \sin(PHr)I_{lod}}{2C_{dc}}$$

$$P_{13} = \frac{M_r \sin(PHr)}{2C_{dc}}, P_{14} = \frac{M_r \cos(PHr)I_{loq}}{2C_{dc}}$$

$$P_{15} = \frac{M_i \cos(PHi)}{2C_{dc}}, P_{16} = -\frac{M_i \sin(PHi)I_{bopd}}{2C_{dc}}$$

$$P_{17} = \frac{M_i \sin(PHi)}{2C_{dc}}, P_{18} = \frac{M_i \cos(PHi)I_{bopq}}{2C_{dc}}$$

$$P_{124} = P_{12} + P_{14}, P_{186} = P_{18} + P_{16}$$

$$q_1 = P_{11}C_{11} + P_{13}C_{15} + P_{15}P_1 + P_{17}P_5$$

$$q_2 = P_{11}C_{10}, q_3 = P_{11}C_{14} + P_{13}C_{17} + P_{15}P_3 + P_{17}P_7$$

$$q_4 = P_9 + P_{11}C_{13} + P_{13}C_{18}, q_5 = P_{11}C_{12} + P_{13}C_{16} + P_{124}$$

$$q_6 = P_{10} + P_{15}P_4 + P_{17}P_8$$

$$q_7 = P_{15}P_2 + P_{17}P_6 + P_{186}$$

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